

Homework

1. Please determine whether the following vectors are linear independent?

$$(1) \quad a_1 = (2, -1, 0, 3), \quad a_2 = (1, 2, 5, -1), \quad a_3 = (7, -1, 5, 8)$$

$$(2) \quad p_1(x) = 1 - x, \quad p_2(x) = 5 + 3x - 2x^2, \quad p_3(x) = 1 + 3x - 2x^2$$

2. Let V be a vector space over \mathbb{R} and $n \in \mathbb{N}$ be an odd number. If the vectors $x_1, x_2, \dots, x_n \in V$ are linearly independent, then the same stands also for the vectors $x_1 + x_2, x_2 + x_3, \dots, x_{n-1} + x_n, x_n + x_1$.